

İzmir Kâtip Çelebi University Department of Engineering Sciences Phy101 Physics I Final Examination January 20, 2025 10:20 – 11:50 Good Luck!

NAME-SURNAME:

SIGNATURE:

ID:

DEPARTMENT:

INSTRUCTOR:

DURATION: 90 minutes

 \diamond Answer all the questions.

 \diamond Write the solutions explicitly and clearly.

Use the physical terminology.

 \diamond You are allowed to use Formulae Sheet.

 \diamond Calculator is allowed.

 \diamond You are not allowed to use any other

electronic equipment in the exam.

 \diamond I declare hereby that I fulfilled the requirements for the attendance according to the University regulations and I accept that my examination will not be valid otherwise.

Question	Grade	Out of
1A		15
1B		20
2		15
3		20
4		15
5		15
TOTAL		100

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- 1. A) A rescue team lifts an injured person directly upward by means of a motor-driven cable. The lift is performed in three stages, each requiring a vertical distance of 10.0 m:
 - 1) The initially stationary person is **accelerated** to a speed of 5.00 m/s;
 - 2) He is then lifted at the constant speed of 5.00 m/s;
 - 3) Finally, he is **decelerated** to zero speed.

How much work is done on the 80.0 kg rescue by the force lifting him during each stage (W_1, W_2, W_3) ?

 $\omega_1 - mgd = \frac{1}{2}$ $\Rightarrow \omega_1 = \frac{1}{2}(80-$ Fid-mgd= W1-mgd= 15 10M 80.06 11 Constant F50 speed 2 :U2-mgd= =mgd= 7.84 kJ iii) Decelerated to 5.0 mls W3-mgd= AK mus, = 6.84 KJ

B) In the figure below, particle 1 of mass $m_1 = 0.40 \ kg$ slides rightward along an x axis on a frictionless floor with a speed of $v_{1i} = 2.0 \ m/s$. When it reaches x = 0, it undergoes a one-dimensional elastic collision with stationary particle 2 ($v_{2i} = 0$) of mass $m_2 = 0.30 \ kg$.



- i Calculate the particle velocities v_{1f} and v_{2f} after the elastic collision.
- ii After the collision, particle 2 reaches a wall at $x_w = 3 m$, it bounces from the wall during which 36% of its kinetic energy is lost (turned into thermal energy). At what position on the x axis does particle 2 collide again with particle 1?

i) Collision at x=0 Elestic collision -> KE is conser 36% KE reaches He 1.339M .375m+1.839m/sx1.2415 0.73M

2. A 10.0 kg block is released from point A in figure. The track is frictionless except for the portion between B and C, which has a length of 6.00 m. The block travels down the track, hits a spring of force constant k = 2250 N/m, and compresses the spring 0.25 m from its equilibrium position before coming to rest momentarily. Determine the coefficient of kinetic friction between the block and the rough surface between B and C.



3. A soccer player kicks a soccer ball of mass 0.45 kg that is initially at rest. The foot of the player is in contact with the ball for 3.0×10^{-3} s, and the force of the kick is given by

$$F(t) = [(6.0 \times 10^6)t - (2.0 \times 10^9)t^2] N$$

for $0 \le t \le 3.0 \times 10^{-3}$ s, where t is in seconds. Find the magnitudes of

- i the impulse on the ball due to the kick,
- ii the average force on the ball from the player's foot during the period of contact,
- iii the maximum force on the ball from the player's foot during the period of contact,
- iv the ball's velocity immediately after it loses contact with the player's foot.

- 4. The angular position of a point on a rotating wheel is given by $\theta(t) = 2.0 + 4.0t^2 + 2.0t^3$, where θ is in radians and t is in seconds. At t = 0,
 - i what is the point's angular position?
 - ii what is its angular velocity?
 - iii what is its angular velocity at t = 4.0 s?
 - iv Calculate its angular acceleration at t = 2.0 s.
 - v Is its angular acceleration constant? Why?

 $G(t) = 2t^3 + 4t^2 + 2$ i) at t=0, 0(\$)=2 rad 2 ii) $w(t) = \frac{d\theta(t)}{dt} = 6t^2 + 8t$, at t = 0, $w(\phi) = \phi(\phi)$ ui) t=4 ~ w(t=4)=6.42+8.4=128 rad/s (3) iv) $\mathcal{L}(t) = \frac{d\omega(t)}{dt} = 12t+8$, at t=2, $\mathcal{L}(t=2) = 32$ rad/s² \mathcal{V} at \mathcal{A} has time dependency \mathcal{D} NOT constant \mathcal{A}

5. A solid ball of radius $R = 0.2 \ m$ and mass $M = 3 \ kg$ is placed at the top of a ramp of height $h = 1.2 \ m$ and $\theta = 37^{\circ}$. (Hint: $I = \frac{2}{5}mR^2$)



- i If the ramp surface is frictionless, calculate the velocity of the ball's center of mass (v_{com}) and its angular velocity (ω) at the bottom of the ramp.
- ii Calculate the minimum value of the coefficient of static friction (μ_s) that would cause smooth rolling (no slipping) of the ball down the ramp. Calculate v_{com} and ω at the bottom of the ramp for this case.

i) frictionless ~ no roll 2 ú 9.8m (0.88s) m= 4.52m



İzmir Kâtip Çelebi University Department of Engineering Sciences Phy101 Physics I Final Examination January 19, 2024 08:30 – 10:00 Good Luck!

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DEPARTMENT:

INSTRUCTOR:

DURATION: 90 minutes

Answer all the questions.
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1B		20
2		15
3		15
4		15
5		20
TOTAL		100

This page is intentionally left blank. Use the space if needed.

1. A) A block, initially at rest, of weight W = 10.0 N is released from the point A moving down an inclined plane with angle $\alpha = 53^{\circ}$. It meets a spring with a spring constant k = 500.0 N/m at the point C and compresses the spring a distance d = 10.0 cm stopping at the point B momentarily. The surface has a coefficient of friction, μ between points A and C. There is no friction between C and B. The distance between A and C, is L = 50.0 cm. Take g = $9.8 m/s^2$.

- a Calculate μ by using the work-kinetic energy theorem.
- b After stopping at B momentarily, the block bounces back and goes up on the incline some distance and stops. What is this stopping distance measured from the point C?

W= DK : Work - Kinetic Ene AK=0 since on= va= of & Sin ~ W=0= mgH-frL-1-kd2 mgH-(10N) (0.5m+ ii) AK=0 since 0 >-mg(x+d)Sind-Mmg 29 X= 2 500 0 (0.1m)2-(10N)(0.1m) Sm 53 = 0.135m (0.76)(10N) Coss3+(10N) SIMS3

B) Consider 'L' shaped plate with uniform mass per unit area σ .



Find the center of mass, \vec{r}_{COM} in unit vector notation.

- 2. A 5.0 g marble is fired vertically upward using a spring gun. The spring must be compressed 8.0 cm, if the marble is to just reach a target 20 m above the marble's position on the compressed spring.
 - i What is the change (ΔU_g) in the gravitational potential energy of the marble-Earth system during the 20 m ascent?
 - ii What is the change (ΔU_s) in the elastic potential energy of the spring during its launch of the marble?
 - iii What is the spring constant of the spring?

3. A 3.2 kg box slides on a horizontal frictionless table and collides with a 2.0 kg box initially at rest on the edge of the table, at height h = 0.40 m. The speed of the 3.2 kg box is 3.0 m/s just before the collision.



If the two boxes stick together because of packing tape on their sides, what is their kinetic energy just before they strike the floor?

Stick Together rampletely inelastic allison 2) v 3 Pi= Pf in n-direction +m2 12i= (m, +m2 +x-direction 1-8 m 3 m/ have 1 alte mpart. n. Now, Conservation of 1 + Ui= Kc+2 $m = m_1 + m_2$ s at a round KE ~ KE= 1 (5.2 kg) (1.8 m/) + (52kg) (9.8m/52) 0.40m = 28.8 5 00

- 4. The angular position of a point on a rotating wheel is given by $\theta(t) = 2.0 + 4.0t^2 + 2.0t^3$, where θ is in radians and t is in seconds. At t = 0,
 - i what is the point's angular position?
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5. In Figure, a solid cylinder of radius 10 cm and mass 12 kg starts from rest and rolls without slipping a distance L = 6.0 m down a roof that is inclined at the angle $\theta = 30^{\circ}$. $(I = 1/2MR^2)$



- i What is the angular speed of the cylinder about its center as it leaves the roof?
- ii The roof's edge is at height H=5.0 m. How far horizontally from the roof's edge does the cylinder hit the level ground?

nservation o h=LSin30 U=RW 6 x Sin 30 ii 0 y-yo= voy t+ 1 gt2 Vox= 406530 $5m - \phi = V_0 Sm 30t$ $4.2t^2 + 3.15t - 5=0$ $2x_0 = V_0 Cos30t$ = 63m/s Cos30 0.74s = 4.03m 2-1.9t2 Suadratiz Equation 3 ti2 = -3.15 +



İzmir Kâtip Çelebi University Department of Engineering Sciences Phy101 Physics I Final Examination May 30, 2022 11:00-12:30 Good Luck!

NAME-SURNAME:

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DEPARTMENT:

INSTRUCTOR:

DURATION: 90 minutes

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1A		15
1B		10
1C		15
2		15
3		20
4		20
5		20
TOTAL		115

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 A) A 2.5 kg block slides into a spring with a spring constant of 320 N/m. When block stops, it has compressed the spring by 7.5 cm. The coefficient friction between the block and the horizontal surface is 0.25.

	2.5 kg	320 N/m
S. C.S.	ELENE EL	AND CHANGER AND CHANGE

What is the block's speed just as the block reaches the spring?

Work-Energy Theorem $\Delta K + \Delta U + \Delta E_{H} = W = 0$ (no enternal $\Delta K = K_{f} - K_{i}$ { $K_{f} = 0$ sine $S_{g} = 0$ & M = 2.5 kg $\Delta U = -W_{S} = \frac{1}{2} kn^{2}$ { k = 320 N/m $M = 7.5 \times 10^{-2} m$ $\Delta E_{th} = f_{h} \mathcal{X} = (M_{h} mg) \mathcal{X} \{ M_{t} = 0.25 \\ \approx \int_{-\frac{1}{2}}^{-\frac{1}{2}} m v_{t}^{2} + \frac{1}{2} k \mathcal{X}^{2} + M_{k} mg \mathcal{X} = 0 \}$ $\begin{array}{c} u_{1}^{2} = \frac{2}{m} \sqrt{\frac{1}{2} k_{x}^{2}} + M_{e} M_{g} \chi = \frac{2}{2 \cdot sk_{g}} \sqrt{\frac{1}{2} 320 M} (7 \cdot s_{N} 0 \cdot m)^{2} \\ = 0.93 \, m/s 0 + (0.25 \cdot 2 \cdot sk_{g} \cdot 9 \cdot 8 m/2) (7 \cdot s_{N} \cdot 10 \cdot m) \end{array}$

B) In Figure, a block of ice slides down a frictionless ramp at angle $\theta = 50^{\circ}$ while an ice worker pulls on the block (via a rope) with a force $\vec{F_r}$ that has a magnitude of 50 N and is directed up the ramp. As the block slides through distance $d = 0.50 \ m$ along the ramp, its kinetic energy increases by 80 J. How much greater would its kinetic energy have been if the rope had not been attached to the block?



 $SK + \Delta U + W = 0$ $S = F \cdot d$ $F \cdot d Cos 180^{\circ}$ I = (SON)(0-Sm) = 2S J $\Delta U = mgh T$ $(\Delta K + 2SJ) + \Delta U = 0$ Increase D = not change D = 0 Coes not change

C) A force $\vec{F} = (cx - 3x^2)\hat{x}$ acts on a particle as the particle moves along an x axis, with \vec{F} in newtons, x in meters, and c a constant. At x = 0, the particle's kinetic energy is 20.0 J; at x = 3.00 m, it is 11.0 J. Find c.

$$\begin{split} & \omega = \int \vec{F} \cdot d\vec{n} = \int \vec{F}_{x} dn = \int (cx - 3x^{2}) dx \\ & (2) & x_{i} & x_{i} & (3) \\ & = \frac{c}{2}x^{2} - x^{3} \Big|_{0}^{3} = 4.5c - 27 & (3) \\ & \omega = \Delta K = K_{f} - K_{i} = 11 - 20 = -95 & (5) \\ & \Rightarrow 4.5c - 27 = -9 & \sim \Rightarrow c = 4.4 \\ & 0 & 0 \\ \end{split}$$

2. Figure below shows an 8.00 kg stone at rest on a spring. The spring is compressed 10.0 cm by the stone.

i What is the spring constant?

ii The stone is pushed down an additional 30.0 cm and released. What is the elastic potential energy of the compressed spring just before that release?

iii What is the change in the gravitational potential energy of the stone-Earth system when the stone moves from the release point to its maximum height?

height?

iv What is that maximum height, measured from the release point?

m = 8 kg y = 0.1m F_{g} O.Im ii) pushed down 0.3m further DK+DU=0 ~ Kf+Uf=Ki+Ui ⇒ k=7841 $\rightarrow \mathcal{U}_{f} = \frac{1}{2} k x^{2} = \frac{1}{2} (784 N/m) (-0.4m)$ iii) at maximum height $\chi_{f} + \mathcal{U}_{f}$ -62.75 i + Ui iv) Uf=mgh=62.75 (Uf= 62.75 $h = \frac{62.75}{m_{g}} = \frac{6.2.75}{(8k_{g})(9.8m/_{s})}$

3. In Figure, a 300 g ball with a speed v of 6.0 m/s strikes a wall at an angle θ of 30° and then rebounds with the same speed and angle. It is in contact with the wall for 10 ms. In unit vector notation, what are



- i the impulse on the ball from the wall,
- ii the average force on the wall from the ball?

G= 4 Cost 2 - 45 MO g = 5.2 2 - 3.0 g (3)rebounds with same speed 10; 1=10; 1 $\vec{J} = \Delta \vec{p} = M \vec{v}_{f} - M \vec{v}_{z} = 2 (0.30 \text{ kg}) (3.0 \text{ m/s}) \hat{f}$ $\vec{3} = (1.8 \text{ Ns}) \hat{f}$ upward ii) $\vec{J} = \vec{F} = 1.8 \ \vec{J} = (180 \ n) \ \vec{J}$ are age force on the $\vec{\Delta t} = \vec{F} = 1.8 \ \vec{J} = (180 \ n) \ \vec{J}$ are age force on the Newton's third law. (180 N) \ average force on the wall from the ball

4. In Figure, block 1 has mass $m_1 = 460 \ g$, block 2 has mass $m_2 = 500 \ g$, and the pulley, which is mounted on a horizontal axle with negligible friction, has radius R=5.00 cm. When released from rest, block 2 falls 75.0 cm in 5.00 s without the cord slipping on the pulley.



In unit-vector notation, what are

- i What is the magnitude of the acceleration of the blocks?
- ii What are tension T_2 and tension T_1 ?
- iii What is the magnitude of the pulley's angular acceleration?
- iv What is its rotational inertia?

=460 Unknoons Ti, Tz, a need one more equation + 75.0 cm in 5-005 the cord di=a = ICC -TZIR ci (4.87-4.5 1.38

5. A solid ball of radius $R = 0.2 \ m$ and mass $M = 3 \ kg$ is placed at the top of a ramp of height $h = 1.2 \ m$ and $\theta = 37^{\circ}$. (Hint: $I = \frac{2}{5}mR^2$)



i If the ramp surface is frictionless, calculate the velocity of the ball's center of mass (v_{com}) and its angular velocity (ω) at the bottom of the ramp.

- ii Calculate the minimum value of the coefficient of static friction (μ_s) that would cause smooth rolling (no slipping) of the ball down the ramp. Calculate v_{com} and ω at the bottom of the ramp for this case.
- iii If the coefficient of kinetic friction (μ_k) between the ball and the ramp surface is 0.1 and it is known that the ball does not roll smoothly down the ramp (there is sliding), calculate v_{com} and ω at the bottom of the ramp.

i) frictionless
$$\rightarrow$$
 no rolling \rightarrow $v_{con} = v \in w = 0$
 $W_f + K_f = U_i + K_i' \rightarrow \frac{1}{2} - m v^2 = Mgh \rightarrow v = /2gh' (1)$
at the bottom $\rightarrow v = /2 + (3 \cdot 8m/2)(12m) = (4 \cdot 85 \cdot m/5) (1)$
ii) smooth rolling a cong $= \frac{9 \cdot 5m \cdot 9}{1 + 1} - (1mR^2) + (5 = -1 - cong - 2mR^2) + (1 + 2mR^2) + (2 +$



İzmir Kâtip Çelebi University Department of Engineering Sciences Phy101 Physics I Final Examination Take Home Assignment Due date: June 05, 2020 10:30 Good Luck!

NAME-SURNAME:

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DEPARTMENT:

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Question	Grade	Out of
TOTAL		100

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1. (Kinetic Energy and Work) A 250 g block is dropped onto a relaxed vertical spring that has a spring constant of k = 2.5 N/cm. The block becomes attached to the spring and compresses the spring 12 cm before momentarily stopping.





What is the speed of the block just before it hits the spring (assume that friction is negligible)?

Answer: v = 3.5 m/s



(Kinetic Energy and Work) An object having a mass of 1 kg, which is initially at rest at point A, starts its motion along frictionless path of A-C and finally, stops momentarily after it compresses the spring (k = 100 N/m) by x m. Take g = 10 m/s².



- i Find the compression distance, x, if angle θ of the inclined plane is 30^{o} and the distance travelled on inclined plane, d, just before hitting the spring is 1.0 m.
- ii The object starts moving in opposite direction after it stops momentarily. What is the speed of the object just after it starts its motion in opposite direction?
- iii Determine the final position of the object at the end of motion in opposite direction along path C A.

Answer: i)
$$x = 0.5 m$$
 ii) $v = 5 m/s$ iii) A



3. (Kinetic Energy and Work) Figure gives the acceleration of a 2.00 kg particle as an applied force F_a moves it from rest along an x-axis from x = 0 to x = 9.0 m. The scale of the figure's vertical axis is set by $a_s = 6.0 m/s^2$.



How much work has the force done on the particle when the particle reaches

i x= 4.0 m,

ii x= 7.0 m,

iii What is the particle's speed and direction of travel when it reaches x = 4.0 m.



ii What is the average and instantaneous angular acceleration for that time interval? 1) a) $w = F x = (mas) x$, $\int 0 \le x \le 4$ (1-5) $6 + 36$ $2kg * 6m/s^2 (1m - 0m) + 2kg \times 6h/s^2 (4m - 1n)$
1) 425 $iii) 0 \le x \le 7$ $biii)$ $biii) 0 = 0 = 0 = 301$ $iii) 0 \le x \le 7$ $bii) 0 = 0 = 0 = 0 = 0 = 0 = 0 = 0 = 0 = 0 $
\tilde{u}) $\frac{1}{2}ma_{f}^{2} = \frac{1}{2}mR_{f}^{2} = \Delta K = 0$ $O = 6.48 \rightarrow 0 = 6.5 m/s + 2 frection$

4. (Kinetic Energy and Work - 40%) A block of mass m = 2.0 kg is dropped from height h = 40 cm onto a spring of spring constant k = 1960 N/m (See the figure below).



Find the maximum distance the spring is compressed.

System: Block + spring + Forth
No external forces =) Machanical energy is conserved

$$K_i + U_i = k_f + U_f$$

(1) $K_{i=0}$, block is dropped.
 $K_f = 0$ to have movimum distance of compression.
(2) $\frac{1}{2}$ $\frac{1$

5. (Kinetic Energy and Work- 40%) A 120 kg mass hangs by vertical rope $L = 3.5 m \log as$ in Figure a. A person then displaces the mass to a position d = 2.0 m sideways from its original position, always keeping the rope taut, and holds it in this new position as in Figure b.



As the mass is moved to this position, how much work is done by the person?

Answer: 738 J



- 6. (Kinetic Energy and Work- 40%) The spring of a spring gun has force constant k = 400 N/55 and negligible mass. The spring is compressed 6.00 cm, and a ball with mass 30.0 g is placed in the horizontal barrel against the compressed spring. The spring is then released, and the ball is propelled out the barrel of the gun. The barrel is 6.00 cm long, so the ball leaves the barrel at the same point that it loses contact with the spring. The gun is held so he barrel is horizontal.
 - i Calculate the speed of the ball as it leaves the barrel if a constant resisting force of 6.00 N acts on the ball as it moves along the barrel.
 - ii What is the greatest speed the ball have along the barrel if a constant resisting force of $6.00 \ N$ acts on the ball as it moves along the barrel?

Answer: i) 4.90 *m/s* ii) 5.20 *m/s*

$$k = 400 \text{ M/m}$$

$$(200000)$$
i) $f \leftrightarrow F_{\text{spring}}, f = 600 \text{ N}$

$$M_{\text{iot}} = K_{f} - K^{2}^{0}$$

$$W_{f} + W_{\text{Fipring}} = \frac{1}{2} \text{ m } v^{2}, \quad W_{f} = \frac{1}{f^{2}x_{0}} = -f^{2}x_{0}$$

$$W_{f} + W_{\text{Fipring}} = \frac{1}{2} \text{ m } v^{2}, \quad W_{f} = \frac{1}{f^{2}x_{0}} = -f^{2}x_{0}$$

$$W_{f} + W_{\text{Fipring}} = \frac{1}{2} \text{ m } v^{2}, \quad W_{f} = \frac{1}{f^{2}x_{0}} = -f^{2}x_{0}$$

$$= -f^{2}x_{0} + \frac{1}{2} \text{ K}x_{0}^{2} = \frac{1}{2} \text{ m } v^{2}$$

$$= -f^{2}x_{0} + \frac{1}{2} \text{ K}x_{0}^{2} = \frac{1}{2} \text{ m } v^{2}$$

$$= (6.00 \text{ N})(0.06 \text{ m}) + \frac{1}{2}(400 \text{ N/m})(0.06 \text{ m})^{2} = \frac{1}{2}(30 \times 10^{3} \text{ kg}) v^{2}$$

$$\frac{1}{10} = 4.90 \text{ m/s}$$
i) The greatest speed occurs when the acceleration (and the net force) ore zero.
$$f \leftrightarrow F_{\text{spring}} \quad \prod_{f=0}^{F} = 0 \implies \text{ Kx} = f$$

$$x = f/k$$

$$W_{f} + W_{\text{spring}} = K_{f} - K^{0}$$

$$= \frac{1}{2} \text{ (M} \text{ M} \text{ m)} (\frac{6.00 \text{ M}}{400 \text{ M/m}})^{2} = \frac{1}{2} (30 \times 10^{-3} \text{ kg}) \cdot \frac{1}{2} \text{ mos} = 5.20 \text{ m/s}$$

7. (Potential Energy and Conservation of Energy) In the figure below, a block slides along a track from one level to a higher level after passing through an intermediate valley. The track is frictionless until the block reaches the higher level. There a frictional force stops the block in a distance d.



The block's initial speed v_0 is 6.0 m/s, the height difference h is 1.1 m, and μ_k is 0.60. Find d.

Answer: d = 1.2 m

System: Shek + Farth + track
No ertained force, then

$$O = \Delta E_{nech} + \Delta E_{th}$$

$$O = \left(\frac{1}{d} - m y_{1}^{t} + mgh\right) - \frac{1}{2} m V_{1}^{2} + f_{k} d$$

$$O = mgh - \frac{1}{2} m V_{1}^{2} + \mu_{k}(mg)d \qquad (F_{k} = ng) \text{ at the hyber live}$$

$$OR you can reach some equation by taking black + Earth as$$

$$a system and having f_{k} as the external force;$$

$$W_{krc} = \Delta E_{nech}$$

$$(Then, solving for J;$$

$$d = \frac{1}{m} \left(\frac{V_{1}^{2}}{2g} - h\right) = \frac{1}{0.50} \left[\frac{(6.0 m_{1})^{2}}{2(9.7 m_{1})} - (1.4 m)\right]$$

$$\Rightarrow \left[\frac{1}{d = 1.2 m}\right]$$

8. (Potential Energy and Conservation of Energy - 40%) Consider the track shown in Figure below. The section AB is one quadrant of a circle of radius 2.0 m and is frictionless. B to C is a horizontal span 3.0 m long with a coefficient of kinetic friction $\mu_k = 0.25$. The section CD under the spring is frictionless. A block of mass 1.0 kg is released from rest at A. After sliding on the track, it compresses the spring by 0.20 m.



Determine the stiffness constant k for the spring.



 $\begin{aligned} \Delta \text{Uint} &= -\text{Wother} \qquad \Delta \text{Uint} : \text{Change in internal energy.} \\ & \text{Wother } : \text{ The work done by forces other than conservative forces (gravitatroad)} \\ \Delta \text{K} + \Delta \text{U} + \Delta \text{Uint} = 0 \quad (\text{low of conservation of energy}) \qquad \qquad \text{elastic force, } \\ & \text{elastic force, } ...) \\ & (\text{Kf} - \text{Ki}) + (\text{Uf} - \text{Ui}) + (-\text{W}_{\text{Ffric.}}) = 0 \quad , \qquad \text{Uf} = \frac{1}{2} \text{K} \times_{\text{max}}^{2} \\ & \text{Uint} = \text{mg} \text{F} \\ & \text{W}_{\text{Ffric.}} = \frac{1}{7} \text{max}^{2} = \frac{1}{2} \text{K} \text{mg} \Delta \text{X} \cos 180^{\circ} \\ & \text{W} = \frac{1}{2} \text{K} \times_{\text{max}}^{2} - \frac{1}{18} \text{cl} \end{aligned}$

9. (Potential Energy and Conservation of Energy - 40%) A 2.00 kg ball is attached to the bottom end of a length of rope with a breaking strength of 44.5 N The top end of the rope is held stationary. The ball is released from rest with the line taut and horizontal ($\theta = 90.0^{\circ}$). At what angle (measured from the vertical) will the rope break? Answer: 40.8°

$$m=2\cos \theta - \Gamma - \mu \sin \theta + \mu \sin \theta = 0$$

$$\sum F_{\Gamma} = m \operatorname{ar}$$

$$\operatorname{Tmox} - mg\cos \theta = m \frac{10^{2}}{\Gamma} \Rightarrow \theta^{2} = \frac{\Gamma}{m} (\operatorname{Tmox} - mg\cos \theta) \operatorname{Cat} + he \operatorname{breaking point})$$

$$E_{\Gamma} = E_{\Gamma}$$

$$E_{\Gamma} = K_{\Gamma} + \mu_{\Gamma}$$

$$\theta = \frac{1}{2}m \theta^{2} + mg \cdot g , \quad g = -\Gamma \cos \theta$$

$$\theta = \frac{1}{2}m (\frac{P}{m} (\operatorname{Tmox} - mg\cos \theta)) - mg \cdot cos \theta$$

$$\theta = \frac{1}{2}m (\frac{P}{m} (\operatorname{Tmox} - mg\cos \theta)) - mg \cdot cos \theta$$

$$\theta = \cos^{-1} (\frac{447 \cdot 5}{3 \cdot 200 \text{ kg}} \cdot 9.80 \text{ m/s}^{2})$$

$$\frac{\Theta}{2} = 40.8^{\circ}$$

10. (Center of Mass and Linear Momentum) A system containing three objects, which is initially at rest, accelerates by the application of a net force. Masses and time dependent position vectors of objects are given as;

Find;

Answer: i) $\vec{r}_{com} = \left[(t^2 - 3t + 24)\hat{i} + (8t - 16)\hat{j} \right] / 12$ ii) $\vec{a}_{com} = \hat{i}/6 \ m/s^2$ iii) $\vec{F}_{net} = 2\hat{i} \ N$

11. (Center of Mass and Linear Momentum) The rigid body shown in figure given below consists of three particles connected by **massless** rods. It is to be rotated about an axis perpendicular to its plane through point P.



If $M = 0.40 \ kg$, $a = 30 \ cm$, and $b = 50 \ cm$, What is the rotational inertia about point P?

Answer: $I = 0.208 \ kgm^2$



12. (Center of Mass and Linear Momentum) A 3.2 kg box slides on a horizontal frictionless table and collides with a 2.0 kg box initially at rest on the edge of the table, at height h = 0.40 m. The speed of the 3.2 kg box is 3.0 m/s just before the collision.



If the two boxes stick together because of packing tape on their sides, what is their kinetic energy just before they strike the floor?

Answer: KE = 29 J

Together mampletely inelastic collision momention in n-direction $+m_2 p_i = (m_1 + m_2) + 3 \vec{p}_i = \vec{p}_i$ = 1.8 m 30 That is the velocity after impair. The progentile motion of Men Kitli=Ketl $m = m_1 + m_2$ & at ground KE ~ KE= 1 (5.2 kg) (1.8 m) (52kg) (9.8m/32) 0.40m = 28.8 5 00

13. (Center of Mass and Linear Momentum) The mass $m_1 = 1.0 \ kg$ moving with a speed $v_1 = 5.0 \ m/s$ on a horizontal frictionless floor collides with a mass $m_2 = 2.0 \ kg$ initially at rest. After the collision, m_1 moves at a speed $v_{1f} = 3.0 \ m/s$ and m_2 moves at a speed v_{2f} along the directions shown in the figure.



iv Find the impulse delivered to m_1 during the collision. Give your answer in terms of unit vector notation.

Answer: i) $v_{2f} = 2.0 \ m/s$ ii) Inelastic iii) $\vec{v}_{com_f} = 5/3 \ m/s \ \hat{i}$ iv) $\vec{J}_1 = (-3.2\hat{i} + 2.4\hat{j}) \ kgm/s$



- 14. (Rotation) The angular position of a point on the rim of a rotating wheel is given by $\theta = 4.0t + 3.0t^2 + t^3$, where θ is in radians and t is in seconds. What are the angular velocities at
 - i t = 2.0 s and t = 4.0s,
 - ii What is the average and instantaneous angular acceleration for that time interval?

Answer: i) $w(t = 2.0 \ s) = 28 \ rad/s \ w(t = 4.0 \ s) = 76 \ rad/s$ ii) 24 rad/s^2

$$\begin{array}{l} \hat{b} = 4.0t + 3.0t^{2} + t^{3} \\ \hat{b} = 4.0t + 3.0t^{2} + t^{3} \\ \hat{c} = \frac{1}{2} \\ \hat{c} = 4.0 + 6.0t + 6.2t^{2} \\ \hat{c} = 4.0s \\ \hat{c} = 4.0s \\ \hat{c} = 4.0s \\ \hat{c} = \frac{1}{2} \\ \hat{c} = \frac{1}{$$

15. (Rotation) In figure, two 6.2 kg blocks are connected by a massless string over a pulley of radius 2.40 cm and rotational inertia $7.40 \times 10^{-4} \ kg.m^2$. The string does not slip on the pulley; it is not known whether there is friction between the table and the sliding block; the pulley axis is frictionless. When this system is released from rest, the pulley turns through 0.650 rad in 91.0 ms and the acceleration of the block is constant. What are



Answer: i) 157.0 rad/s ii) 3.8 m/s² iii) $T_1 = 37.4 \text{ N iv}$ $T_2 = 32.6 \text{ N}$







16. (Rotation - 40%) In figure, a wheel of radius 0.20 m is mounted on a frictionless horizontal axle. A massless cord is wrapped around the wheel and attached to a 2.0 kg box that slides on a frictionless surface inclined at angle $\theta = 20^{\circ}$ with the horizontal. The box accelerates down the surface at 2.0 m/s^2 .



17. (Rotation - 40%) The reel shown in Figure has radius $R = 0.300 \ m$ and moment of inertia $I = 1.00 \ kg.m^2$. One end of the block of mass $m = 0.500 \ kg$ is connected to a spring of force constant $k = 50.0 \ N/55$, and the other end is fastened to a cord wrapped around the reel. The reel axle and the plane having an inclination of $\theta = 37^{\circ}$ are frictionless. The reel is wound counterclockwise so that the spring stretches a distance $d = 0.200 \ m$ from its unstretched position and is then released from rest.



Find the angular speed of the reel when the spring is again unstretched.

Answer: $1.74 \ rad/s$



18. (Rotation - 40%) A $m_1 = 15.0 \ kg$ object and a $m_2 = 10.0 \ kg$ object are suspended, joined by a cord that passes over a pulley with a radius of $R = 10.0 \ cm$ and a mass of $M = 3.00 \ kg$ as seen in the Figure.



The cord has a negligible mass and does not slip on the pulley. The pulley rotates on its axis without friction. The objects start from rest $d = 3.00 \ m$ apart. Treat the pulley as a uniform disk, and determine the speeds of the two objects as they pass each other. **Hint:** $I_{CM} = \frac{1}{2}MR^2$

Answer: 2.36 m/s



19. (Rolling, Torque, and Angular Momentum) A hollow cylinder of outer radius $R = 5 \ cm$ and mass $M = 50 \ g$ with moment of inertia about the center of mass $I_{com} = MR^2$ starts from rest and moves down an incline tilted at an angle $\theta = 20^{\circ}$ from the horizontal. The center of mass of the cylinder has dropped a vertical distance $h = 30 \ cm$ when it reaches the bottom of the incline. The coefficient of static friction between the cylinder and the surface is μ_s . The cylinder rolls without slipping down the incline. **Answer: i)** $\mu_s > 0.18$ **ii)** $v = 1.7 \ m/s$



- i What is the minimum value for the coefficient of static friction μ_s such that the cylinder rolls without slipping down the incline plane?
- ii What is the magnitude of the velocity of the center of mass of the cylinder when it reaches the bottom of the incline?



20. (Rolling, Torque, and Angular Momentum - 40%) In figure given below, a constant horizontal force \vec{F}_{app} of magnitude 12 N is applied to a uniform solid cylinder by fishing line wrapped around the cylinder. The mass of the cylinder is 10 kg, its radius is 0.10 m, and the cylinder rolls smoothly on the horizontal surface. (**Hint**: $I_{COM} = \frac{1}{2}MR^2$)

Fishing line

- i What is the magnitude of the acceleration of the center of mass of the cylinder?
- ii What is the magnitude of the angular acceleration of the cylinder about the center of mass?
- iii In unit-vector notation, what is the frictional force acting on the cylinder?

 $cw \rightarrow as positive (as our choice!)$ (1) $T_p = T_{com} + InR^2 = \frac{1}{2}MR^2 + MR^2 = \frac{3}{2}MR^2$ 9(71) Fapp=12N M=10 kg =2R=C=Ipx-= 2R Fapp= (3 rolls smoothly d=16 rad /2

21. (Rolling, Torque, and Angular Momentum - 40%) The radius of the roll of paper shown in Figure is 7.6 cm and its moment of inertia is $I = 3.3 \times 10^{-3} \ kg.m^2$. A force of 2.5 N is exerted on the end of the roll for 1.3 s, but the paper does not tear so it begins to unroll. A constant friction torque of 0.11 m.N is exerted on the roll which gradually brings it to a stop.



Assuming that the paper's thickness is negligible, calculate

- i the length of paper that unrolls during the time that the force is applied $(1.3 \ s)$ and
- ii the length of paper that unrolls from the time the force ends to the time when the roll has stopped moving.

Answer: i) 1.56 m ii) 1.13 m



22. (Rolling, Torque, and Angular Momentum - 40%) A 500 g bird is flying horizontally at 2.24 m/s, not paying much attention, when it suddenly flies into a stationary vertical bar, hitting it $d = 25.0 \ cm$ below the top as seen in the Figure. The bar is uniform, $l = 0.750 \ m$ long, has a mass of 1.50 kg, and is hinged at its base. The collision stuns the bird do that it just drops to the ground afterward (but soon recovers to fly happily away).



Answer: i) 2.00 rad/s ii) 6.58 rad/s

- i) Angular momentum is conserved in the collision between the bird and the bar: $L_{i}^{2} = L_{f}^{2}$ $m \mathcal{V}(L-d) = \left(\frac{1}{3}ML^{2}\right) \mathcal{W} \quad (\text{for the axis at hinge})$ $\mathcal{W} = \frac{3m\mathcal{V}}{ML^{2}}(L-d) = \frac{3(0.5 \text{ kg})(2.24 \text{ m/s})(0.750 \text{ m} - 0.250 \text{ m})}{(1.5 \text{ kg})(0.750 \text{ m})^{2}}$ $\mathcal{W} = 2.00 \text{ rad/s}$
- ii) Energy is conserved in the motion of the bar ofter the collision; $E_{I} = E_{L}$ $\frac{1}{2} I W_{1}^{2} + Mg \frac{1}{2} = \frac{1}{2} I W_{2}^{2} , \quad I = \frac{1}{3} M L^{2}$ $\frac{1}{2} \left(\frac{1}{3} M L^{2}\right) W_{1}^{2} + Mg \frac{1}{2} = \frac{1}{2} \left(\frac{1}{3} M L^{2}\right) W_{2}^{2}$ $W_{2} = \sqrt{W_{1}^{2} + \frac{3g}{L}} = \sqrt{(2.00) rad/s}^{2} + \frac{3(9.80 m/s^{1})}{(0.750 m)} = 6.58 rad/s.$

İzmir Kâtip Çelebi University Department of Engineering Sciences Phy101 Physics I Final Examination May 22, 2019 10:30 – 12:30 Good Luck!

IZMIR

NAME-SURNAME:

SIGNATURE:

ID:

DEPARTMENT:

INSTRUCTOR:

DURATION: 120 minutes

Answer all the questions.
Write the solutions explicitly and clearly.
Use the physical terminology.
You are allowed to use Formulae Sheet.
Calculator is allowed.

◊ You are not allowed to use any other

electronic equipment in the exam.

◊ I declare hereby that I fulfilled the requirements for the attendance according to the University regulations and I accept that my examination

will not be valid otherwise.

Question	Grade	Out of
1A		15
1B		15
2		20
3		20
4		20
5		20
TOTAL		110

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1. A) A force $\vec{F} = (cx - 3x^2)\hat{x}$ acts on a particle as the particle moves along an x axis, with \vec{F} in newtons, x in meters, and c a constant. At x = 0, the particle's kinetic energy is 20.0 J; at x = 3.00 m, it is 11.0 J. Find c.

$$\begin{split} & \omega = \int \vec{F} \cdot d\vec{x} = \int \vec{F}_{x} dx = \int (cx - 3x^{2}) dx \\ & (2) & x_{i} & x_{i} & (3) \\ & = \frac{c}{2}x^{2} - x^{3} \Big|_{0}^{3} = 4.5c - 27 \\ & \omega = \Delta K = K_{f} - K_{i} = 11 - 20 = -95 \\ & \Rightarrow 4.5c - 27 = -9 \\ & \sim \right\} c = 4 \\ & M_{m} \\ \hline & 0 \\ \hline \end{split}$$

- B) You drop a 2.00 kg physics book to a friend who stands on the ground at distance D=10.0 m below. If your friend's outstretched hands are at distance d=1.50 m above the ground (see Figure),
- i How much work Wg does the gravitational force do on the book as it drops to her hands?
- ii What is the change ΔU in the gravitational potential energy of the book– Earth system during the drop?

If the gravitational potential energy U of that system is taken to be zero at ground level,

- iii what is U when the book is released?
- iv what is U when it reaches her hands?
- v Now take U to be 100 J at ground level and again find Wg, ΔU , U at the release point, and U at her hands.



i) $W_{g} = F_{g} \cdot d = mg dCos \Theta \int d = 10m - 1.5m = 8.5m$ = $(2kg)(9.8m/z) 8.5mCos0^{\circ} \Theta = 0^{\circ}$ $\vec{u} = \frac{1675}{\Delta u} = \frac{1675}{4} = m_g(y_f - y_c) = (2k_g)(9.8m/s^2)(1.5m-10m)$ iii) Ui=mgy;=(2kg)(9.8m/s2)10m=1965 iv) 295 $W_{g} = 1675, \Delta u = -1675, U_{i} = mgy_{i} + 1005$ $= \frac{296 J}{U_{f} = m_{g} y_{f} + 100 J}$ = 129 j

- 2. A rod of length 30.0 cm has linear density (mass per length) given by $\lambda = 50.0 \frac{g}{m} + 20.0 x \frac{g}{m}$ where x is the distance from one end, measured in meters.
 - i What is the mass of the rod?
 - ii How far from the x = 0 end is its center of mass?

0.3 0. 2 1dx = (50+20x) 5 15. Xdm 6 Xcm = 120 × 2 -= 0.15

3. A soccer player kicks a soccer ball of mass 0.40 kg that is initially at rest. The foot of the player is in contact with the ball for 2.0×10^{-3} s, and the force of the kick is given by

$$F(t) = \left[(12.0 \times 10^9)t^2 - (4.0 \times 10^{12})t^3 \right] N$$

for $0 \le t \le 2.0 \times 10^{-3}$ s, where t is in seconds. Find the magnitudes of

- i the impulse on the ball due to the kick,
- ii the average force on the ball from the player's foot during the period of contact,
- iii the maximum force on the ball from the player's foot during the period of contact,
- iv the ball's velocity immediately after it loses contact with the player's foot.

$$\begin{array}{c|c} m=0.45 \text{ kg} & (i) \ J=? \ \text{impulse} \quad \overline{f_{ay}} = \frac{J}{\Delta t} \quad ck \quad J = \int F(t) dt = \int (6x10^{6}t - 2x10^{9}t^{2}) dt \\ \Rightarrow J = 3x10^{6}t^{2} - \frac{2x10^{9}}{3}t^{3} \left[\frac{3x10^{73}}{3} - \frac{3}{3}x10^{5}(9x1)\frac{5}{5} \right] - \frac{3}{3}x10^{5}(27x10^{3}) \left[\frac{-9}{4} - 9x(5) \right] \\ contact times = \\ 3x0x10^{3}s \\ \hline tu) \quad \overline{f_{av}} = \frac{J}{\Delta t} = \frac{9Ns}{3^{10}x10^{3}s} = \frac{3x10^{5}}{3^{10}x10^{3}s} - \frac{3}{2}x10^{5}(27x10^{3}) \left[\frac{-9}{4} - 9x(5) \right] \\ contact times = \\ 3x0x10^{3}s \\ \hline tu) \quad \overline{f_{av}} = \frac{J}{\Delta t} = \frac{9Ns}{3^{10}x10^{3}s} = \frac{3x10^{5}}{3^{10}x10^{3}s} = \frac{3x10^{5}}{2} \left[\frac{0}{10} \\ \hline tu) \quad \overline{f_{av}} = \frac{J}{3^{10}x10^{3}s} = \frac{3x10^{5}}{3^{10}x10^{3}s} = \frac{3x10^{5}}{2} \left[\frac{0}{10} \\ \hline tu) \quad \overline{f_{av}} = \frac{J}{3^{10}x10^{5}s} \\ \hline dF(t) \quad \overline{f_{av}} = \frac{9}{6}x10^{6} - 4x10^{5}t = 0 \\ \Rightarrow f(t-1.5x10^{3}s) = f_{av}} = \frac{6x10^{6}(1.5x10^{3}) - 2x10^{9}(1.5x10^{3})^{2}}{10} \\ \hline f_{av} = \frac{J}{2} \\ cu \\ \Delta \overline{p} = \overline{f_{5}} - \overline{f_{1}} = m\overline{u_{5}} - m\overline{u_{5}} \\ \Rightarrow \Delta p = m\overline{u_{5}} = 3 \\ \hline u = 20 \\ m \\ \end{array}$$

- 4. The angular position of a point on a rotating wheel is given by $\theta(t) = 2.0 + 4.0t^2 + 2.0t^3$, where θ is in radians and t is in seconds. At t = 0,
 - i what is the point's angular position?
 - ii what is its angular velocity?
 - iii what is its angular velocity at t = 4.0 s?
 - iv Calculate its angular acceleration at t = 2.0 s.
 - v Is its angular acceleration constant?

 $G(t) = 2t^3 + 4t^2 + 2$ i) at t=0, 0(\$)=2 rad 2 ii) $w(t) = \frac{d\theta(t)}{dt} = 6t^2 + 8t$, at t = 0, $w(\phi) = \phi(\phi)$ ui) t=4 ~ w(t=4)=6.42+8.4=128 rad/s (3) iv) $\mathcal{L}(t) = \frac{d\omega(t)}{dt} = 12t+8$, at t=2, $\mathcal{L}(t=2)=32$ rad/s² \mathcal{V} at has time dependency \mathcal{D} NOT constant 3

- 5. A uniform ball, of mass M = 6.0 kg and radius R, rolls smoothly from rest down a ramp at angle $\theta = 30.0^{\circ}$ (see Figure, $I = \frac{2}{5}MR^2$)
- i The ball descends a vertical height h = 1.20 m to reach the bottom of the ramp. What is its speed at the bottom?
- ii What are the magnitude and direction of the frictional force (f_s) on the ball as it rolls down the ramp?



 $\begin{array}{c|c} M=6kg \\ \textcircled{O}=30^{\circ} \\ I=\frac{2}{5}mR^{2} \\ h=1.2m \end{array} \xrightarrow{(i)} Mechanical Energy is conserved for the ball-enth system \\ & & & \\ \overrightarrow{F_{N}} \ & & \\ \hline S \ & & \\ \hline S \ & & \\ \hline M \ & & \\ \hline S \ & & \\ \hline M \ & & \\ \hline S \ & & \\ \hline S \ & & \\ \hline M \ & & \\ \hline S \ & & \\ \hline S \ & & \\ \hline M \ & & \\ \hline S \ & & \\ \hline S \ & & \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline M \ & & \\ \hline M \ & & \\ \hline S \ & & \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline M \ & & \\ \hline M \ & & \\ \hline S \ & & \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline M \ & & \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline M \ & & \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline \end{array} \xrightarrow{(i)} MR^{2} \\ \hline$ 7 1 ven = Mgh ~ v= 10 g =4-11/5 Newton's 2rd law in x-direction - $MgSin30^{\circ} + f_{s} = Ma_{com,x}$ Newton's 2nd low in angular form $Z_{net} = I_{com} \propto n_{p} f_{s}R = \frac{2}{5}MR^{2}x$ acomy = - XR ~ 5 fs = - Macony x $= 7 - Mg Sim 30^\circ + f_s = -\frac{5}{2} f_s \rightarrow f_s = \frac{2}{7} Mg Sim 30^\circ$ = = (6kg)(98N/2) 1= 8.4N